

Grades 3-5

Supporting the Integration of Mathematical Content in K-5 ELD Classroom

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Objectives

- Make connections between Arizona's English Language Proficiency Standards (ELPS) and the Mathematical Practices
- Reflect on current practices
- Discuss strategies to support teachers in increasing the use of academic vocabulary and student discussions in the ELD classroom

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AZCCRS Require

- Language development as a complex process
- Language development aimed at effective communication
- Disciplinary language that goes beyond technical vocabulary to build the communicative competence necessary for participation in disciplinary practices

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Implications for Instruction

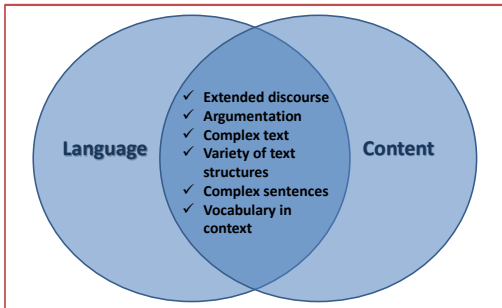
- All students will need to read, write, speak & listen extensively
- The focus of the classroom will need to shift to engage students in disciplinary discourse practices
- Language activities will need to include opportunities to involve students with a variety of modes, representations, types of texts, types of talk, and different audiences

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What does it mean to utilize content?

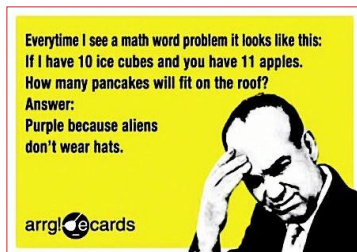


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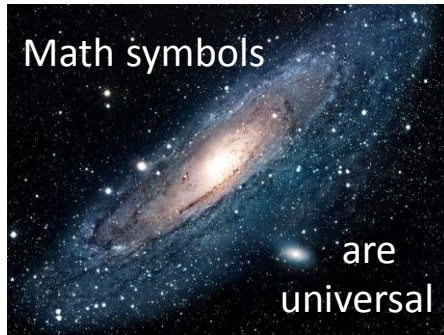
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What Makes This Complex for ELLs?



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Syntax in Mathematics

"4 is 2 less than 6"

4 is 4 =
2 less than 6 2 - 6

$4 = 2 - 6$

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Mathematical Text

Julie has $\frac{1}{3}$ more apples than Lucy. Julie has 16 apples. How many apples does Lucy have?



Reference Table 1 CCSS-M

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Fist-to-Five



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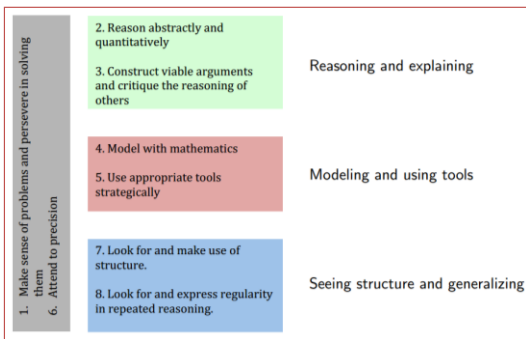
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Mathematical Practices

1. Make sense of problems and persevere in solving them
2. Reason abstractly and quantitatively
3. Construct viable arguments and critique the reasoning of others
4. Model with mathematics
5. Use appropriate tools strategically
6. Attend to precision
7. Look for and make use of structure
8. Look for and express regularity in repeated reasoning

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Mathematical Practice 1

Make sense of problems and persevere in solving them

- *Explain* the meaning of the problem
- *Plan* a solution pathway
- *Determine* if the solution is reasonable and accurate
- *Explain* correspondences among models, pictures, diagrams, equations, verbal descriptions, tables, and graphs

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Mathematical Practice 3

Construct viable arguments and critique the reasoning of others

- *Explain* the reasoning underlying a strategy, solution or conjecture
- *Arguments* may rely on definitions, previous results, properties or structure
- *Present* your arguments
- *Articulate* and *Justify* generalizations
- *Listen to* or *Read* arguments of others. Ask questions to clarify or improve the argument.
- *Communicate* their arguments, *compare* them to others as well as *respond* to the critiques of others

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Mathematical Practice 6

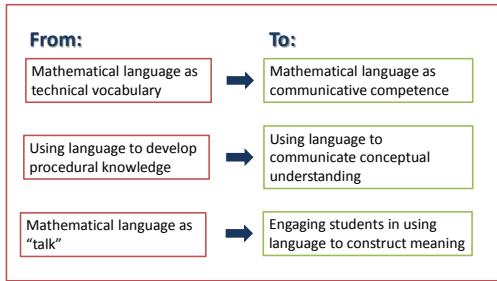
Attend to Precision

- *Formulate* precise explanations
- *Use* math vocabulary
- *Use* appropriate labels to *communicate* the meaning of the representation
- *Record* their work

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Shifts in the Usage of Language for Math



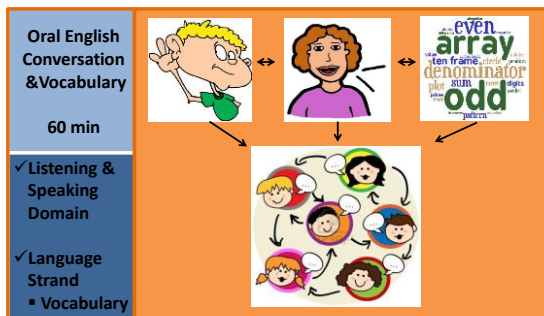
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Time Allocations and Standards

Time Allocations	Reading	Oral English Conversation & Vocabulary	Writing	Grammar
	60 min	60 min	60 min	60 min
Standards to Use	✓ Reading Domain	✓ Listening & Speaking Domain ✓ Language Strand ▪ Vocabulary	✓ Writing Domain	✓ Language Strand ▪ Grammar

Time Allocations and Standards



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Oral English Conversation & Vocabulary Connection

Academic Language consists of **academic vocabulary** and is used in **academic discourse**.

Academic Language includes:

- The language used in the classroom and workplace
- The language of text
- The language of assessment
- The language of academic success
- The language of power



Academic vocabulary is critical to understanding the concepts taught in school. It includes both specialized content vocabulary and high frequency precise vocabulary.



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Academic discourse is a structured dialogue that provides students with the vocabulary and syntax needed to discuss topics using academic language in meaningful contexts.



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Stage		ELL Stage II: Grades 1-2				
Standard		Language Strand			Domain	
Standard 2: The student will acquire English language vocabulary and use it in relevant contexts.						
Pre-Emergent		Emergent		Basic	Low Intermediate	High Intermediate
Proficiency Levels						
PE-1: repeating and grouping the names of common objects or pictures into basic given categories with instructional support. <small>(math, science, social studies)</small>		E-1: naming and grouping common objects and pictures into given categories with instructional support. <small>(math, science, social studies)</small>		B-1: naming and grouping common objects and pictures with self-selected categories and providing rationale. <small>(math, science, social studies)</small>	LI-1: classifying common words into basic conceptual categories (colors, shapes, foods) and providing rationale. <small>(math, science, social studies)</small>	HI-1: classifying words into conceptual categories and providing rationale. <small>(math, science, social studies)</small>
PE-2: repeating sight words. <small>(math, science, social studies)</small>		E-2: recognizing sight words with instructional support. <small>(math, science, social studies)</small>		B-2: recognizing sight words. <small>(math, science, social studies)</small>	LI-2: identifying the meaning of and using sight words. <small>(math, science, social studies)</small>	HI-2: identifying the meaning of and using sight words. <small>(math, science, social studies)</small>
Performance Indicators						
PE-3: repeating high frequency words. <small>(math, science, social studies)</small>		E-3: recognizing high frequency words with instructional support. <small>(math, science, social studies)</small>		B-3: recognizing and identifying the meaning of high frequency words with instructional support. <small>(math, science, social studies)</small>	LI-3: identifying the meaning of and using high frequency words. <small>(math, science, social studies)</small>	HI-3: identifying the meaning of and using high frequency words. <small>(math, science, social studies)</small>

Connections to Mathematical Practices



Kinder Video: Table Talk

1. What performance indicator is this instruction addressing?
2. Which mathematical practice is this instruction supporting?

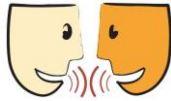


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First Grade Video: Table Talk

1. What performance indicator is this instruction addressing?
2. Which mathematical practice is this instruction supporting?



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Describe

1. Distribute your cards among the members of your group.
2. Do not show your card.
3. Take turns describing your card using as much detail as possible.

Sentence Frames:

- My picture shows...
- It has ___ parts and...
- It does not have
- My graphic contains ___
- My ___ was created by...

Mathematical Terminology:

square multiple horizontal
quadrilateral area vertical
perimeter line array

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Sequence

Once all of the cards have been described, decide on an order that makes sense and place the cards.

- Do not look at cards.
- Each person needs to decide where to place their card and provide the rationale for their decision.



Sentence Frames:

- I have the (first, next, last) card because....
- My card should be ____ in the sequence because...
- My ____ (follows, proceeds) ____ because...



Describe and Explain

Independently, In Pairs, or Small Groups

Analyze the Sequence. Take notes and be prepared to discuss your analysis:

- How do you see the shapes growing?
- Can you see it more than one way?
- Can the way you “see” the sequence growing help you determine the next arrangement?

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Reasoning and Argumentation

Which has more volume:

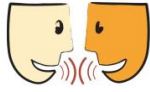
100 pounds of feathers or 100 pounds of bricks?



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Table Talk



1. How did this activity engage you with the mathematical practices, processes, and language?
2. How did the activity support and challenge ELLs?
3. What kind of supports will teachers need to implement instruction that develops complex language through meaningful use of content?

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Language for Classroom Discussion

	Casual Conversational English	Formal Spoken & Written English
Sharing Personal Ideas or Opinions	<ul style="list-style-type: none"> • I think... • I learned that... 	<ul style="list-style-type: none"> → I decided that ... → I believe that ... → I concluded that ... → I observed that ...
Pointing Out Similarities	<ul style="list-style-type: none"> • Mine's the same. • Oh yeah. Right. • Me too. 	<ul style="list-style-type: none"> → My idea is similar to ___'s. → My idea builds upon ___'s. → I agree with ___. → I also think that ___.
Expressing Agreement	<ul style="list-style-type: none"> • Yeah. Right. • Uh huh. 	<ul style="list-style-type: none"> → I agree with ___'s idea that ... → I support ___'s decision to ... → Like ___, I support ...
Asking for Clarification & Paraphrasing	<ul style="list-style-type: none"> • Huh? • What? • I don't get it. 	<ul style="list-style-type: none"> → I don't quite understand. → Could you explain what you mean by ___ → If I understand you correctly, you are saying that ___

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Final Thoughts

- ELLs must have opportunities to engage in quality, sustained, deep interactions to build knowledge.
- Dialogue involves the exchange of ideas and is not dominated by one party.
- Dialogue between peers builds on participant's ideas to promote improved understanding of concepts.
- Knowledge is jointly constructed through the use of language.
- Talk is about the subject matter of the discipline and encourages reasoning, application of ideas, argumentation, forming generalizations, and asking questions.

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